

## Errata and updates for ASM Exam C/Exam 4 Manual (Seventeenth Edition Third Printing) sorted by date.

- [5/25/2017] On page 143, on the second and third lines of the answer to Example 8G, change 1.174 to 1.1774.
- [1/13/2017] On page 1112, in exercise 56.15, on the last line of the table, delete “Claims”.
- [1/5/2017] On page 149, in the heading of Table 82., change Meaaures to Measures.
- [12/14/2016] On page 759, on the third line of Section 38.5, replace “Section 38.5” with “Section 35.5”.
- [12/8/2016] On page 63, on the second line of the answer to Example 4E, replace 1dx with 1 dt.
- [11/24/2016] On pages 681–682, replace the solution to exercise 34.32 beginning with the third paragraph with the following:

If you aren’t comfortable calculating the Erlang distribution function, an alternative method for calculating  $\Pr(Z > 20)$ , is to calculate it directly. Once again,  $Z = X_1 + X_2$ , where  $X_1$  and  $X_2$  are the two exponential observations. We want  $\Pr(Z > 20)$ . By the Law of Total Probability, conditioning on  $X_1$ ,

$$\Pr(Z > 20) = \int_0^{\infty} \Pr(Z > 20 \mid X_1 = x_1) f_{X_1}(x_1) dx_1 \quad (*)$$

The integral’s lower bound is 0 since  $Z$  cannot be less than 0.  $X_1$  is exponential with mean 6, so

$$f_{X_1}(x_1) = \frac{e^{-x_1/6}}{6} \quad x_1 \geq 0$$

$\Pr(Z > 20 \mid X_1 = x_1)$  is equal to 1 if  $X_1 \geq 20$ , since  $X_2 \geq 0$  and  $Z = X_1 + X_2$ . If  $X_1 < 20$ , then  $Z > 20$  only if  $X_2 \geq 20 - X_1$ . Since  $X_2$  is exponential with mean 6,

$$\Pr(X_2 \geq 20 - x_1) = e^{-(20-x_1)/6}$$

We can now rewrite equation (\*) as follows:

$$\begin{aligned} \Pr(Z > 20) &= \int_0^{20} \Pr(Z > 20 \mid X_1 = x_1) f_{X_1}(x_1) dx_1 + \int_{20}^{\infty} \Pr(Z > 20 \mid X_1 = x_1) f_{X_1}(x_1) dx_1 \\ &= \int_0^{20} e^{-(20-x_1)/6} \left( \frac{e^{-x_1/6}}{6} \right) dx_1 + \int_{20}^{\infty} \frac{e^{-x_1/6}}{6} dx_1 \end{aligned}$$

Let’s evaluate these two integrals.

$$\begin{aligned} \Pr(Z > 20) &= \int_0^{20} \frac{e^{-20/6}}{6} dx_1 + e^{-20/6} \\ &= \frac{20}{6} e^{-20/6} + e^{-20/6} \\ &= \left( 1 + \frac{20}{6} \right) e^{-20/6} \\ &= \frac{13}{3} e^{-10/3} = \boxed{0.154587} \end{aligned}$$

- [11/15/2016] On page 1430, in the solution to question 30, replace  $\mathbf{E}[(X - 10,000)_+] - \mathbf{E}[(X - 500)_+]$  with  $\mathbf{E}[(X - 500)_+] - \mathbf{E}[(X - 10,000)_+]$ .

- [11/13/2016] On page 445, in the solution to exercise 26.3, on the last line, change  $\sqrt{0.1699}$  to  $\sqrt{0.001699}$ .
- [10/30/2016] On page 114, in the solution to exercise 6.23, on the second line, replace disribution with distribution. On the last line, remove the extra equals sign before the final answer.
- [9/30/2016] On page 94, in the solution to exercise 5.14, on the second line, change “between 21 and 25” to “between 20 and 25”.
- [8/28/2016] On page 30,  $F_X(x)$  is not a legitimate distribution function. Replace the example with  
Claim sizes  $X$  initially follow a distribution with distribution function:

$$F_X(x) = 1 - \frac{1}{e^{0.01x}(1 + 0.01x)} \quad x > 0$$

Claim sizes are inflated by 50% uniformly.

Calculate the probability that a claim will be for 60 or less after inflation.

Replace the answer with

Let  $Y$  be the increased claim size. Then  $Y = 1.5X$ , so  $\Pr(Y \leq 60) = \Pr(X \leq 60/1.5) = F_X(40)$ .

$$F_X(40) = 1 - \frac{1}{1.4e^{0.4}} = \boxed{0.5212}$$

- [8/28/2016] On page 158, on the last line, replace 21.2847 with 21.2848.
- [6/29/2016] On page 510, in the solution to exercise 28.9, two lines from the end, delete the extra right parenthesis from the numerator  $e^{-3/12}$ .
- [6/15/2016] On page 410, in the solution to exercise 24.10, on the fourth line, change 48 to 49.
- [6/15/2016] On page 1155, in the solution to exercise 58.16, on the second displayed line, change  $6.52686 \times 10^9$  to  $3.95616 \times 10^9$ . On the next line, change 6.52686 to 3.95616. Change the last 4 lines of the solution to

$$\begin{aligned} \text{Var}(X_3) &= \mathbf{E}[\text{Var}(X_3 | I)] + \text{Var}(\mathbf{E}[X_3 | I]) \\ &= 0.637070(15,187,500) + 0.362930(18,750,000) + (0.637070)(0.362930)(2500 - 2250)^2 \\ &= 16,494,889 \end{aligned}$$

The standard deviation is  $\boxed{4061}$ . (A)

None of the answer choices is correct.

- [5/1/2016] On page 1159, on the third line of the third paragraph, replace “add  $\frac{1}{2}$ ” with “subtract  $\frac{1}{2}$ ”.
- [4/15/2016] On page 1063, replace the first displayed line with

$$\bar{X} = \frac{c_1 + c_2 + c_3}{(6/12) + (8/12) + (3/12)}$$

- [4/11/2016] On page 1026, in the solution to exercise 51.37, on the third displayed line, replace EPV with VHM. On the fourth displayed line, replace VHM with EPV.
- [3/28/2016] On page 1149, in exercise 58.16, ignore the answer choices. The correct answer is not one of the choices.
- [3/7/2016] On page 771, in exercise 38.23, in the table, the sum for interval  $(0, 2,000]$  should be 38,065.

[3/2/2016] On page 664, 12 lines from the bottom, replace the displayed line with

$$\sum_{i=1}^n (\bar{x} - \mu')(2x_i - \mu' - \bar{x}) = (\bar{x} - \mu')(2n\bar{x} - n\mu' - n\bar{x}) = n(\bar{x} - \mu')^2$$

[2/20/2016] On pages 573–574, in the solution to exercise 31.28, on the second-to-last line of the page, the exponent  $\gamma$  should be  $1/\gamma$ . On the first line of page 574, there should be parentheses around the fraction  $\frac{206}{0.8^{-1}-1}$ .

[2/13/2016] On page 1099, on the fourth line, remove the E and the left and right brackets in the numerator of the fraction.

[2/8/2016] On page 630, in the solution to exercise 33.3, on the first line, change “1, 2, and 4” to “1, 3, and 4”.

[2/6/2016] On page 1113, in exercise 56.18, in the table’s fourth column first row, change  $\bar{x}_j$  to  $\bar{x}_i$ .

[1/26/2016] On page 1518, in the solution to question 34, change  $m$  to  $\hat{m}$  in the three places it appears in the solution.

[1/25/2016] On page 270, in the solution to exercise 15.19, on the second displayed line, change  $\leq 0.9$  to  $\geq 0.9$ .

[1/25/2016] On page 787, in the paragraph before Section 39.1, on the first line, change “three” to “two”. On the second-to-last line, change “fifth” to “fourth”.

[1/25/2016] On page 1063, on the line after the first displayed equation, delete the left parenthesis.

[1/25/2016] On page 1342, question 11 is based on material in *Loss Models* that is not on the current syllabus. Replace the question with the following question:

You are given the following information for a group policyholder regarding actual aggregate losses and the variance of aggregate losses in each of 3 years:

	Average Losses Per Member	Number of Members
Year 1	10	4
Year 2	9	5
Year 3	11	10

An exposure unit is defined as a member-year. The expected process variance per unit is 20 and the variance of the hypothetical means per unit is 1.

The prior value of expected losses per member-year is 15.

Calculate the Bühlmann-Straub estimate of aggregate losses per member-year.

- (A) 12.4                      (B) 12.5                      (C) 12.6                      (D) 12.7                      (E) 12.8

[1/25/2016] On page 1496, replace the solution to question 11 with the following solution to the revised question:

The total number of exposures is  $4 + 5 + 10 = 19$ . The weighted observed mean is

$$\bar{X} = \frac{4(10) + 5(9) + 10(11)}{19} = 10.26316$$

The credibility factor is

$$Z = \frac{19}{19 + 20/1} = \frac{19}{39}$$

The Bühlmann-Straub estimate is

$$\frac{19}{39}(10.26316) + \frac{20}{39}(15) = \boxed{12.6923} \quad (\text{D})$$

[1/20/2016] On pages 1491–1492, while the solution to question 33 is correct, the following solution may be clearer:

The likelihood of no deaths is  $(1 - q)^2$ . The prior distribution is normal with density  $f(q)$ . The posterior density function is the likelihood times the prior density, divided by the integral of the likelihood times the prior density. In other words, the posterior density function is

$$\pi(q | N_1) = \frac{(1 - q)^2 f(q)}{\int_{-\infty}^{\infty} (1 - q)^2 f(q) dq} = \frac{(1 - q)^2 f(q)}{\mathbf{E}_Q[(1 - Q)^2]}$$

where  $N_1$  is the observed number of deaths in the first year. The mean of the posterior distribution is

$$\begin{aligned} \mathbf{E}[Q | N_1] &= \frac{\int_{-\infty}^{\infty} q(1 - q)^2 f(q) dq}{\mathbf{E}(1 - Q)^2} \\ &= \frac{\mathbf{E}[Q(1 - Q)^2]}{\mathbf{E}[(1 - Q)^2]} \\ &= \frac{\mathbf{E}[(1 - (1 - Q))(1 - Q)^2]}{\mathbf{E}[(1 - Q)^2]} \\ &= \frac{\mathbf{E}[(1 - Q)^2] - \mathbf{E}[(1 - Q)^3]}{\mathbf{E}[(1 - Q)^2]} \end{aligned}$$

$1 - Q$  is normal with mean 0.995 and variance 0.000001. So

$$\begin{aligned} \mathbf{E}[1 - Q] &= \mu = 0.995 \\ \mathbf{E}[(1 - Q)^2] &= \mu^2 + \sigma^2 = 0.995^2 + 0.000001 = 0.990026 \end{aligned}$$

To obtain  $\mathbf{E}[(1 - Q)^3]$ , we'll use the fact that a normal distribution is symmetric, so that its third central moment is 0.

$$\begin{aligned} \mathbf{E}[(1 - Q) - 0.995]^3 &= 0 \\ \mathbf{E}[(1 - Q)^3] - 3\mathbf{E}[(1 - Q)^2](0.995) + 2(0.995)^3 &= 0 \\ \mathbf{E}[(1 - Q)^3] &= 3\mathbf{E}[(1 - Q)^2](0.995) - 2(0.995)^3 = 3(0.990026)(0.995) - 2(0.995)^3 = 0.985078 \end{aligned}$$

The posterior expected value is

$$\frac{0.990026 - 0.985078}{0.990026} = \boxed{0.004998} \quad (\text{E})$$

[1/17/2016] On page 470, on the last line of the answer to Example 27E, change the denominator 4 to 3.

[12/18/2015] On page 1411, in the solution to question 16, on the fourth line, remove the negative sign in front of  $e^{-1000/\theta}$ ; change  $u = -e^{-1000/\theta}$  to  $u = e^{-1000/\theta}$ .

[11/10/2015] On page 511, in the solution to exercise 28.14, in the table, for Policy 3, change the entry under "End of" from 12-1-2012 to 12-31-2012.

[11/1/2015] On page 229, in the solution to exercise 13.16, on the last line, change the denominator  $e^{\lambda-1}$  to  $e^{\lambda} - 1$ .

[5/29/2015] On page 1552, in the solution to question 19, on the fifth line, change  $e^{-\ln 4}$  to  $e^{\ln 4}$ .